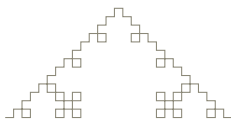


Stock Market Fluctuations: The role of macroeconomic fundamentals, habit and heterogeneous beliefs.

Costas Xiouros

BI Norwegian Business School



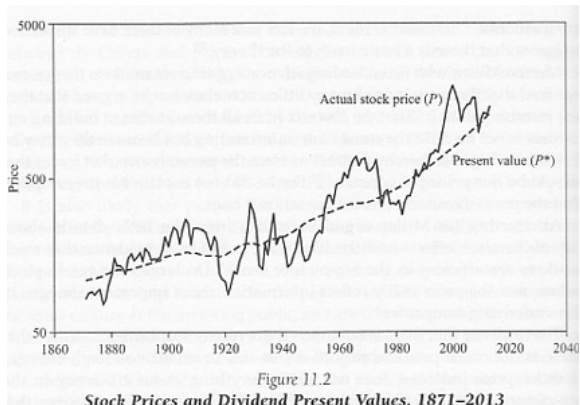
BI - Kleivia Research Meeting

April 7, 2016

Motivation

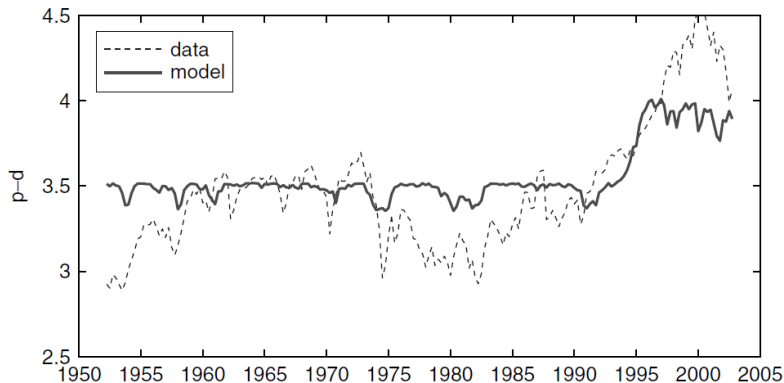
- ⊢ Volatility puzzle of Shiller (1981) and Leroy and Porter (1981).
 - ⤵ Stock market fluctuations are too high, compared to variations in the present value of future dividends, if discount rates are constant.
- ⊢ Price-dividend ratio variance decomposition by Cochrane (1992)
 - ⤵ Bulk of stock market fluctuations due to changes in discount rates, which must have unusual characteristics.
- ⊢ Lettau, Ludvigson and Wachter (2008)
 - ⤵ The unusual rise in the stock-market during the 1990s was due to a decline in equity premium (discount rate), because of a decline in macroeconomic risk.

Shiller: Irrational Exuberance



Lettau, Ludvigson and Wachter (2008)

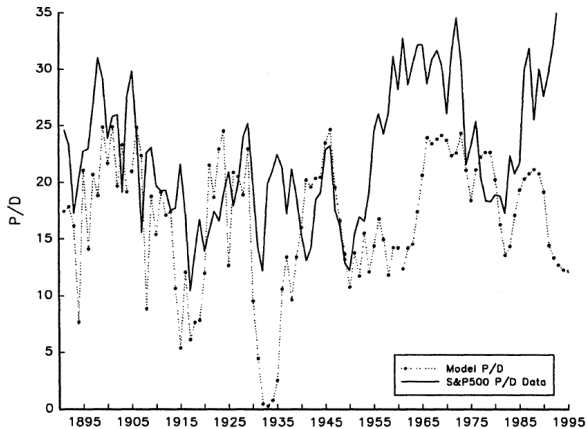
Structural shift in macroeconomic risk.



Equilibrium asset pricing theories

- ‡ Campbell and Cochrane (1999): Time-varying risk-aversion from habit-formation preferences (Sundaresan (1989), Constantinides (1990))
- ‡ Bansal and Yaron (2004): Small and persistent changes in expected consumption growth with Epstein and Zin (1989, 1991) and Weil (1989) preferences.
- ‡ Rare disasters (Barro (2006)) with varying disaster probability (Gabaix (2012), Wachter (2013))
- ‡ Lettau, Ludvigson and Wachter (2008): Time-varying macroeconomic risk

Campbell and Cochrane (1999)



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- ⊢ Fit the model over the period 1947Q1 to 2012Q4

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- ⌋ Findings
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 - ⤵ A decline in heterogeneous beliefs captures well the increase in prices during the 1990s

Model without heterogeneous beliefs

Model with heterogeneous beliefs

Other related literature

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 - Fama and French (2002), Soderlind (2009)

The model: Beliefs

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- ‡ Agents potentially disagree about the conditional mean but agree on the conditional volatility and have the same uncertainty about the mean

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$$\mu_t \mid \mathcal{F}_t \sim N(\mu_t^i, u_t^2)$$

- For each agent the conditional uncertainty about next periods aggregate consumption growth is given by

$$g_{t+1} \mid \mathcal{F}_t \sim N(\mu_t^i, \sigma_t^2 + u_t^2)$$

The model: Preferences

- Agents have identical (multiplicative) habit formation preferences

$$U_i(c, X) = \mathbb{E}_0^i \left[\sum_{t \in \mathbb{N}} \delta^t u(c_t, X_t) \right]$$

where

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and $\eta \leq \gamma$ and $\gamma > 0$.

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- X denotes the common external habit, the log of which follows the process

$$x_{t+1} = \lambda_x x_t + (1 - \lambda_x) y_t$$

where $\lambda_x \in (0, 1)$ and y denotes the log aggregate consumption.

Homogeneous beliefs: Beliefs

- Let us consider first the case of no heterogeneity where agents have some form of adaptive beliefs

$$\begin{aligned}\mu_{t+1} &= \lambda_{\mu}\mu_t + (1 - \lambda_{\mu})g_{t+1}, \\ \sigma_{t+1}^2 &= \lambda_{\sigma}\sigma_t^2 + (1 - \lambda_{\sigma})(\mu_t - g_{t+1})^2.\end{aligned}$$

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- The uncertainty about the conditional mean, consistent with Bayesian updating (of a random walk process) and the previous assumption, is as follows

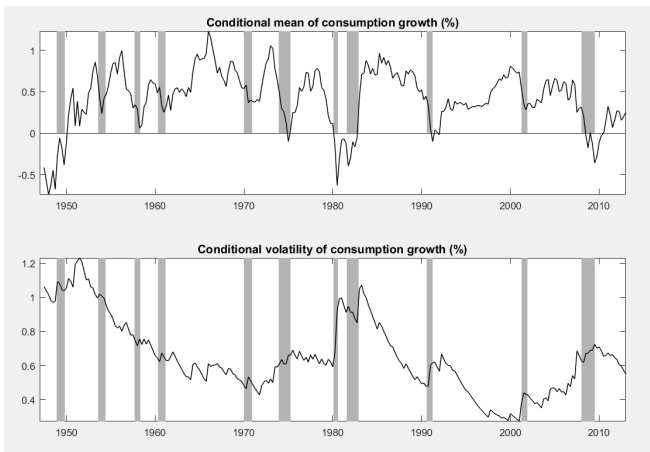
$$\lambda_\mu = \frac{\sigma_t^2}{\sigma_t^2 + u_t^2}, \quad \Rightarrow \quad u_t = \sigma_t \sqrt{\frac{1}{\lambda_\mu} - 1}$$

Consumption growth process estimation

Unconstrained (quasi)-maximum likelihood estimation

	μ_0	σ_0	λ_μ	λ_σ	$\ln L$
g	-0.4131 (0.6520)	1.0627 (0.3015)	0.7840 (0.0614)	0.9098 (0.0216)	-955.6165 -

Fitted mean and volatility of consumption growth



Homogeneous beliefs: Asset prices

- The stochastic discount factor is as follows:

$$M_{t,t+1} = \delta \exp[-\gamma g_{t+1} + (1 - \lambda_x)(\gamma - \eta)\omega_t].$$

under the common beliefs

$$g_{t+1} \sim N\left(\mu_t, \frac{1 - \lambda_\mu}{\lambda_\mu} \sigma_t^2\right)$$

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- The risk-free rate

$$r_t^f = -\log(\delta) + \gamma\mu_t - (1 - \lambda_x)(\gamma - \eta)\omega_t - \frac{1}{2}\gamma^2 \sigma_t^2 \frac{1 - \lambda_\mu}{\lambda_\mu}.$$

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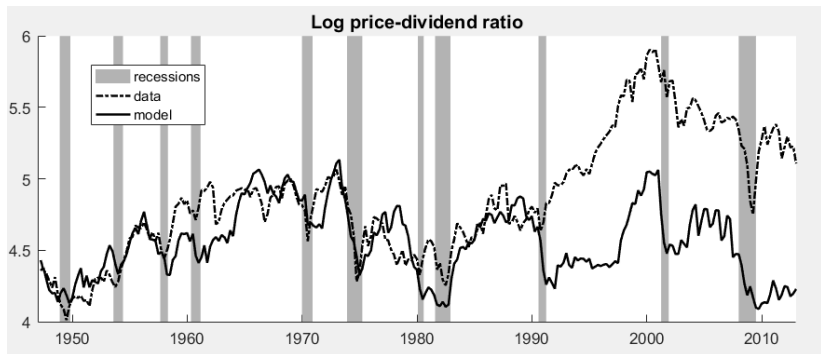
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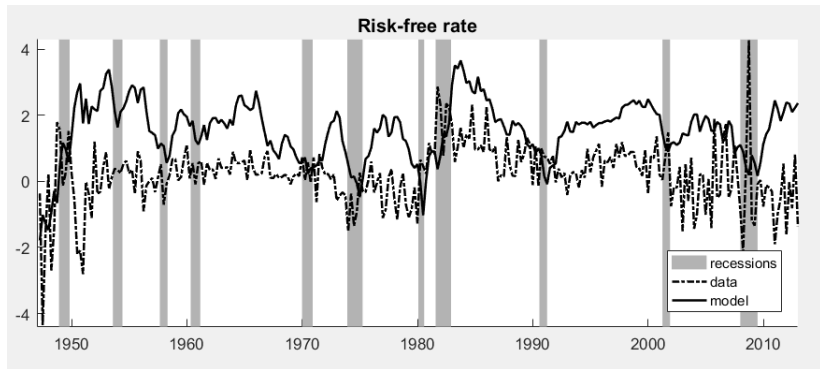
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- The stock market is the claim to the aggregate consumption.

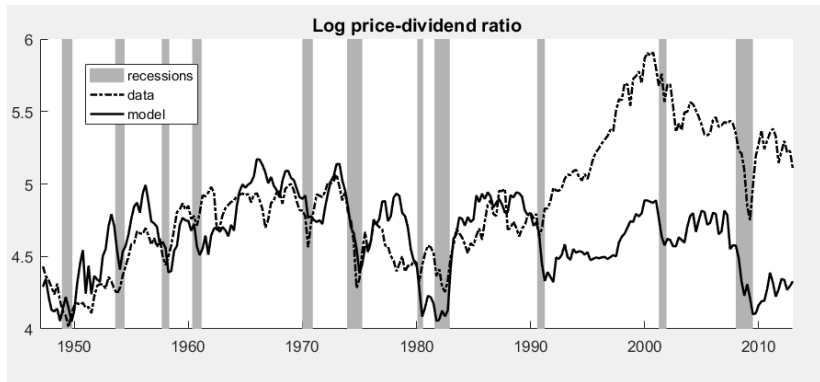
Homogeneous beliefs: Fitted asset prices



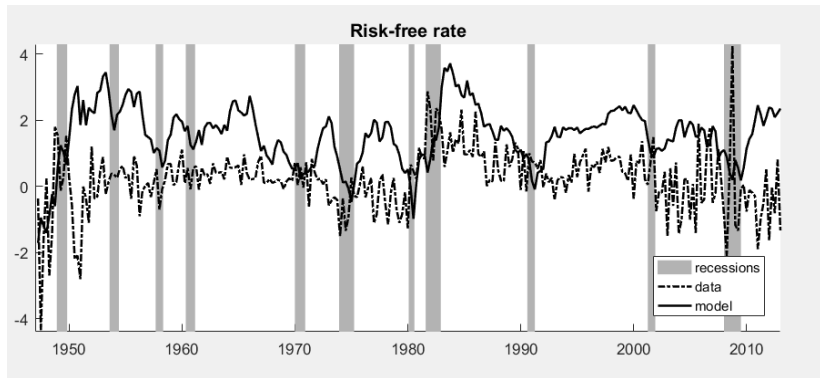
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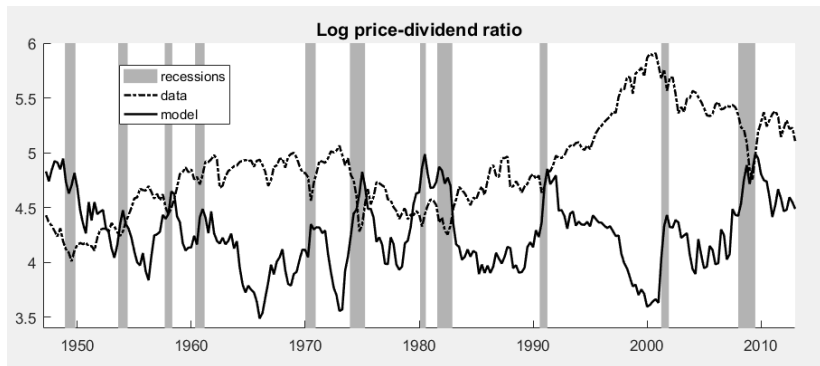
Homogeneous beliefs (remove σ_t): Fitted asset prices



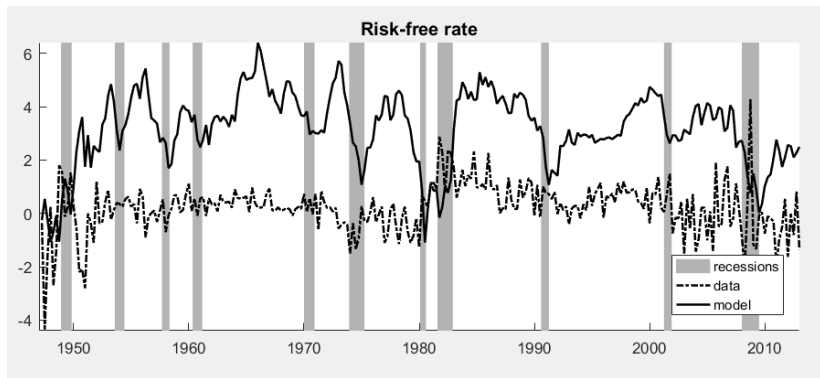
Homogeneous beliefs (remove σ_t): Fitted risk-free rate



Homogeneous beliefs (remove ω_t): Fitted asset prices

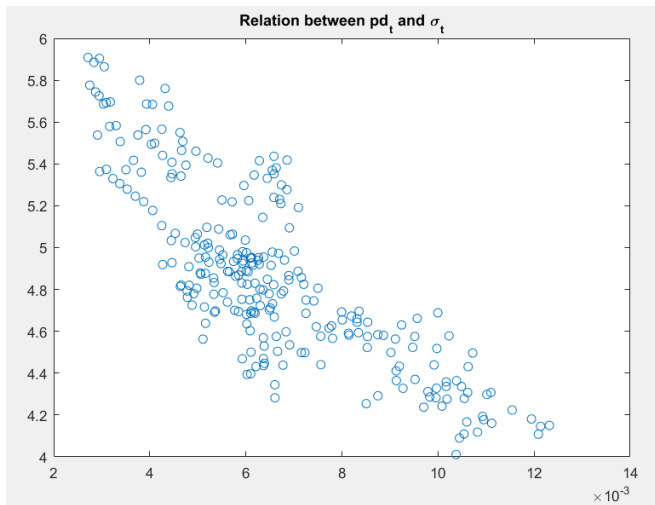


Homogeneous beliefs (remove ω_t): Fitted risk-free rate



Empirical relation: pd_t vs fitted σ_t

Correlation = -0.81



Heterogeneous beliefs: Beliefs

- Individual beliefs differ from the “mean beliefs”

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$$\int \alpha_t^i \mu_t^i di = \mu_t$$

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- The heterogeneity is captured by the cross-section variation in beliefs

$$\nu_t^2 = \int \alpha_t^i (\mu_t^i - \mu_t)^2 di$$

Heterogeneous beliefs: Trading and Aggregation

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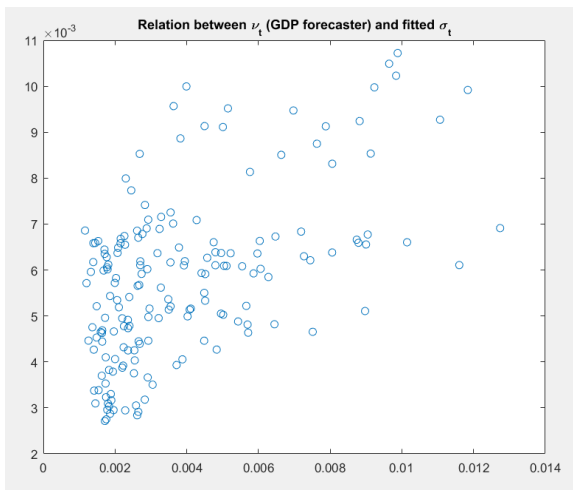
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- The cross-sectional heterogeneity is a function of uncertainty

$$\log(\nu_t) = \kappa_0 + \kappa_1 \log(\sigma_t)$$

Empirical relation between ν and fitted σ

Cross-sectional heterogeneity in GDP forecasts by professional forecasters (Philadelphia Fed). Relation: $y = -0.57 + 0.99x + e$.



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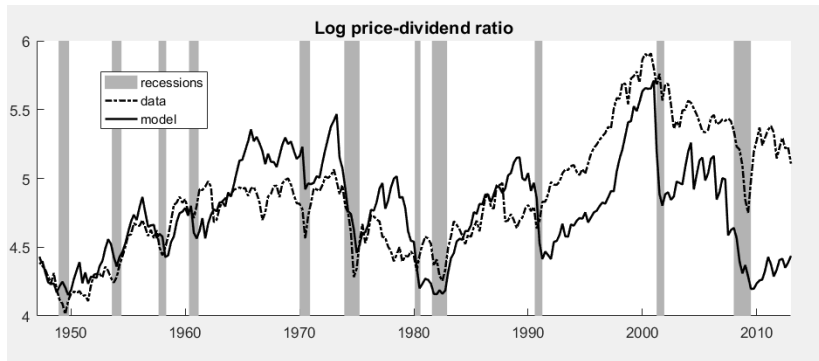
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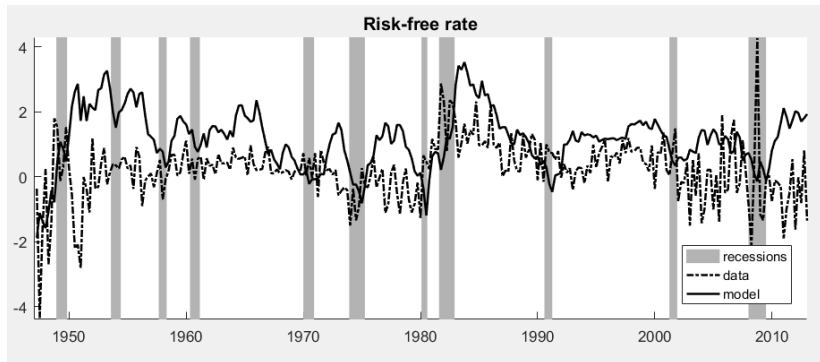
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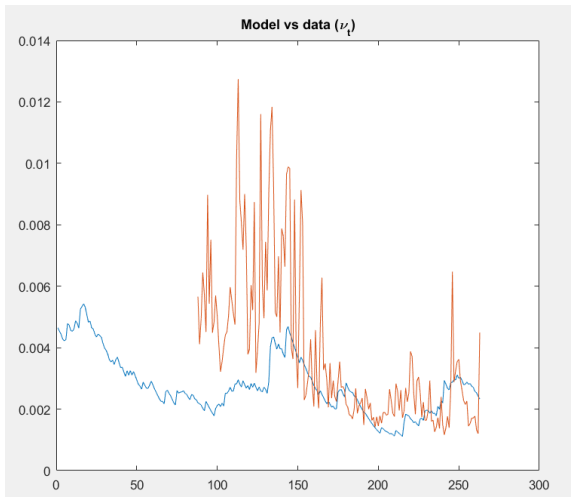
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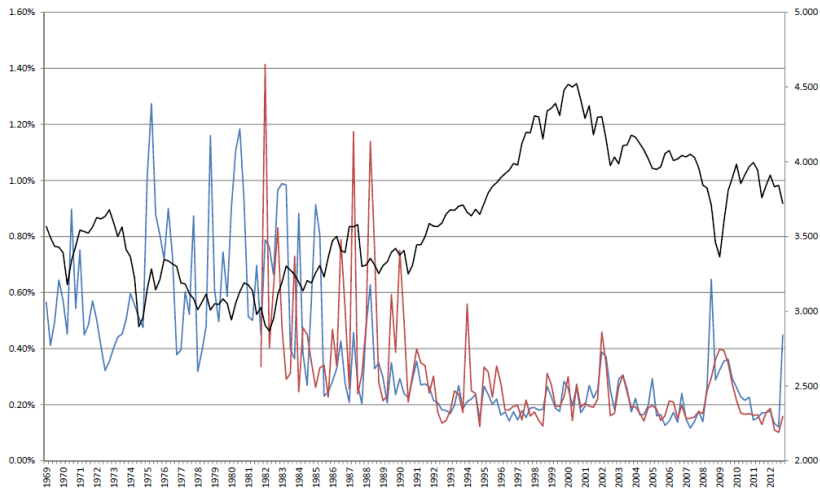
Relation between model heterogeneity and data



Asset pricing moments

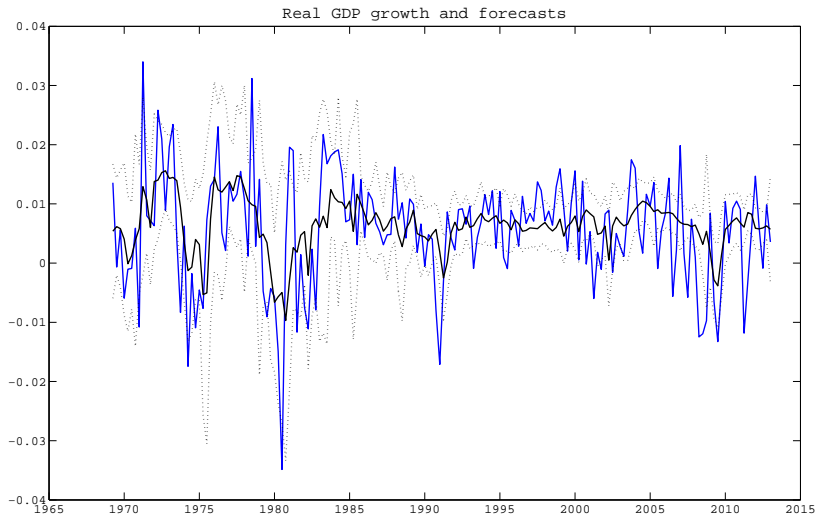
	Data	Hom (all)	Hom ($-\sigma_t$)	Data ($-\omega_t$)	Het (all)
$\mu(pd)$	4.87	4.56	4.63	4.26	4.76
$\sigma(pd)$	0.42	0.25	0.26	0.33	0.36
$ac_1(pd)$	0.98	0.95	0.94	0.92	0.96
$\rho(pd, pd^d)$	-	0.33	0.24	-0.36	0.57
$\mu(r_f)$	0.22	1.53	1.54	3.16	1.15
$\sigma(r_f)$	0.93	0.89	0.89	1.39	0.90
$ac_1(r_f)$	0.35	0.89	0.89	0.90	0.90
$\rho(r_f, r_f^d)$	-	0.14	0.14	0.07	0.13
$\rho(pd, r_f)$	0.05	0.28	0.38	-0.95	0.09
$\mu(r_m)$	1.67	1.61	1.60	1.94	1.51
$\sigma(r_m)$	8.35	8.54	9.26	12.63	10.28
$\mu(r_m - r_f)$	1.45	0.08	0.07	-1.23	0.36
$\sigma(r_m - r_f)$	8.29	8.46	9.19	12.35	10.18

Forecast dispersion and stock prices (corr = -0.68)



Conclusions

Mean and dispersion in analysts' forecasts (Phil. Fed)



Mean and dispersion in analysts' forecasts (Phil. Fed)

